Haskell: Making Types

Principles of Programming Languages

Colorado School of Mines

https://lambda.mines.edu
Review the LGA with your group. Yadda yadda yadda.
In Haskell, using the data keyword lets us define our own types. For example, consider the Bool type, which could be defined as so:

```haskell
data Bool = True | False
```

This reads, the data type Bool can be the value True or False.
Suppose we wanted to define a Point type which stores two Floats:

```haskell
data Point = Point Float Float
```

That `Point` on the RHS of the `=` is the name of the constructor. This could be a different name than the type, but typically you will find it shares the same name.
Suppose we wanted to define a Point type which stores two Floats:

```haskell
data Point = Point Float Float
```

That Point on the RHS of the = is the name of the constructor. This could be a different name than the type, but typically you will find it shares the same name.

To make a Point:

```haskell
(Point 10.5 11.2)
```
While it is true you could just use a \((\text{Float, Float})\) tuple to represent your points, consider the downsides:

- **Type Safety:** What about \((\text{Float, Float})\) tuples that don’t refer to points? Should these work in your methods made for points?
- **Readability:** Would another programmer reading your code understand that the 2-tuple referred to points? Maybe for points but harder for other types (what about a type `Person` that describes features of a person?)
data Shape = Circle Point Float | Rectangle Point Point

We can refer to our type in our functions by pattern matching:

\[ \text{area :: Shape} \rightarrow \text{Float} \]
\[ \text{area} (\text{Circle} \_ r) = \pi \times r^2 \]
\[ \text{area} (\text{Rectangle} \ (\text{Point} \ x1 \ y1) \ (\text{Point} \ x2 \ y2)) = (x2 - x1) \times (y2 - y1) \]

Activity

With your learning group, write a perimeter function. Then, extend the Shape data type to allow for a triangle (how you store this is up to you, right triangles are OK) and extend your perimeter function.
You could imagine writing functions to help you get the center or radius of a Circle:

center (Circle c _) = c
radius (Circle _ r) = r

Fortunately, you don’t have to do this. Haskell provides a Record Syntax that defines these functions for you, and makes your code a bit more readable:

data Circle = Circle { center :: Point, radius :: Float }

This also gives us access to a new constructor syntax:

Circle {center=(Point 1 1), radius=10}
Type parameters allow your type to take another data type. A simple example is the Maybe type builtin to Haskell:

```haskell
data Maybe a = Nothing | Just a
```

How does this read? Maybe is either Nothing or the type specified by `a`.

As another example, suppose you wanted to define a 3D Vector data type that could work on any type:

```haskell
data Vector a = Vector a a a
```
Suppose we want to be able to print our circles to the screen:

```haskell
data Point = Point Float Float deriving (Show)

data Circle = Circle { center :: Point, radius :: Float } deriving (Show)
```

Now...

```
GHCi> Circle (Point 1 1) 1
Circle (Point 1 1) 1
```

We can use this to derive other attributes:

```haskell
data Point = Point Float Float deriving (Show, Eq)
```
How are lists really defined?

One of the most fundamental types in programming languages is the **cons cell**. A cons cell is simply an ordered pair where either element may be a pointer to another.

Haskell uses cons cells to make lists as shown in the image above. In fact, `[42,69,113]` is really just a fancy syntax for `42:69:113:nil`!
Recursive Types

Suppose we wanted to make our own list type:

```haskell
data List a = Empty | Cons a (List a)
```

Then, we can build "lists" using this notation:

- Equivalent to \([5]\)
  \((\text{Cons } 5 \text{ Empty})\)

- Equivalent to \([4,5]\)
  \((\text{Cons } 4 \text{ (Cons } 5 \text{ Empty}))\)

- Equivalent to \([3,4,5]\)
  \((\text{Cons } 3 \text{ (Cons } 4 \text{ (Cons } 5 \text{ Empty)}))\)
Suppose we wanted to make our own list type:

```haskell
data List a = Empty | Cons a (List a)
```

Then, we can build "lists" using this notation:

- __Equivalent to [5]__
  - `(Cons 5 Empty)`

- __Equivalent to [4,5]__
  - `(Cons 4 (Cons 5 Empty))`

- __Equivalent to [3,4,5]__
  - `(Cons 3 (Cons 4 (Cons 5 Empty)))`

What do we get if we rename `Cons` to `:` and `Empty` to `[]`?
Activity: Tree Type

With your learning group, create a Tree type that defines a binary tree.

**Hint:** Go back to our cons cell definition.

Once done, think about how you could extend the type to support $n$-ary trees.